Factor  $x^2 - x - 12$ .

Solution. We must find factors of 12 whose

algebraic sum will be the coefficient of x, which is -1. Choose -4 and +3:

$$x^2 - x - 12 =$$

$$(x-4)(x+3)$$

(x-4)(x+3). Check FOIL answer

Problem 4. Factor. Again, the order of the factors does not matter.

a) 
$$x^2 + 5x + 6 =$$

$$(x+2)(x+3)$$

b) 
$$x^2 - x - 6 =$$

$$(x-3)(x+2)$$

c) 
$$x^2 + x - 6 =$$

$$(x+3)(x-2)$$

d) 
$$x^2 - 5x + 6 =$$

$$(x-3)(x-2)$$

e) 
$$x^2 + 7x + 6 =$$

$$(x+1)(x+6)$$

f) 
$$x^2 - 7x + 6 =$$

$$(x-1)(x-6)$$

g) 
$$x^2 + 5x - 6 =$$

$$(x-1)(x+6)$$

h) 
$$x^2 - 5x - 6 =$$

$$(x+1)(x-6)$$

Problem 5. Factor.

a) 
$$x^2 - 10x + 9 =$$

$$(x-1)(x-9)$$

b) 
$$x^2 + x - 12 =$$

$$(x+4)(x-3)$$

c) 
$$x^2 - 6x - 16 =$$

$$(x - 8)(x + 2)$$

d)  $x^2 - 5x - 14 = ($ 

$$(x-7)(x+2)$$

e) 
$$x^2 - x - 2 =$$

$$(x+1)(x-2)$$

f) 
$$x^2 - 12x + 20 =$$

$$(x - 10)(x - 2)$$

g) 
$$x^2 - 14x + 24 =$$

$$(x - 12)(x - 2)$$

 $\textbf{Solution}. \ \ \text{To factor completely means to first remove any} \underline{\hspace{0.5cm}} GCF$ 

Problem 6. Factor completely. First remove any common factors.

a) 
$$x^3 + 6x^2 + 5x = x(x^2 + 6x + 5) = x(x+5)(x+1)$$

b) 
$$x^5 + 4x^4 + 3x^3 = x^3(x^2 + 4x + 3) = x^3(x+1)(x+3)$$

c) 
$$x^4 + x^3 - 6x^2 = x^2(x^2 + x - 6) =$$
  $x^2(x+3)(x-2)$ 

d) 
$$4x^2 - 4x - 24 = 4(x^2 - x - 6) =$$
  $4(x+2)(x-3)$ 

e) 
$$2x^3 - 14x^2 - 36x = 2x(x^2 - 7x - 18) = 2x(x+2)(x-9)$$

f) 
$$12x^{10} + 42x^9 + 18x^8 = 6x^8(2x^2 + 7x + 3) = 6x^8(2x + 1)(x + 3)$$
.

## 2nd Level

Example 4. Factor by making the **leading term** positive.

$$-x^2 + 5x - 6 = -(x^2 - 5x + 6) = -(x - 2)(x - 3).$$

Problem 7. Factor by making the leading term positive.

a) 
$$-x^2 - 2x + 3 = -(x^2 + 2x - 3) = -(x + 3)(x - 1)$$

b) 
$$-x^2 + x + 6 = -(x^2 - x - 6) = -(x + 2)(x - 3)$$

c) 
$$-2x^2 - 5x + 3 = -(2x^2 + 5x - 3) = -(2x - 1)(x + 3)$$